



# Chapter 1

## Mechanisms

MCT 251

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### 1.1. Definitions



#### □ Reference frame

The coordinates frame considered as a reference.

#### □ Ground

The link which is fixed (no-moving) with respect to reference frame.

- The reference frame may be moving (e.g. automobile chassis of a crane).

#### □ Link

A rigid body, which is the primary element of a mechanism.

#### □ Kinematic pair (pair)

A joint between links in contact to enable a relative motion between these links.

#### □ Kinematic chain

A of links connected through kinematic pairs.

## 1.1. Definitions (cont.)



### ❑ Closed kinematic chain

A kinematic chain in which the links form a loop.

### ❑ Mechanism

A closed kinematic chain with one fixed link.

### ❑ Machine

A mechanism used to modify energy or do a useful work.

### ❑ Degrees of freedom (D.O.F.) of a link

The number of independent coordinates necessary to determine its position.

- No. of D.O.F. of a link in space = 6
- No. of D.O.F. of a link in plane = 3

## 1.1. Definitions (cont.)



### ❑ Degrees of freedom (D.O.F.) of a chain

The number of independent coordinates necessary to determine the positions of its links.

### ❑ Crank

The link which is pivoted to ground, and makes a complete revolution.

### ❑ Lever (rocker)

The link which is pivoted to ground, and makes an oscillatory motion (back and forth).



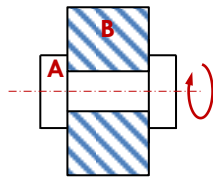
## 1.2. Kinematic pairs

### □ Types of pairs

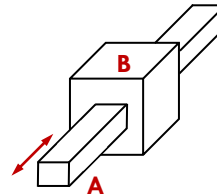
#### ➤ Lower pair

- The kinematic pair enables a relative motion which is defined by one coordinate (e.g. turning and sliding pairs).

- Turning pair



- Sliding pair



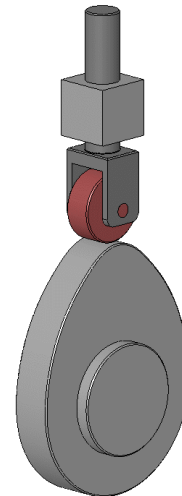
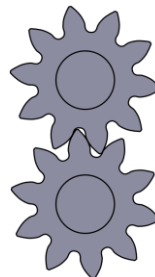
## 1.2. Kinematic pairs (cont.)



### □ Types of pairs

#### ➤ Higher pair

- The kinematic pair enables a relative motion which is defined by two independent coordinates in case of plane chains. (cam and gear pairs).





## 1.2. Kinematic pairs (cont.)

### □ Degrees of freedom lost by pairing

#### ➤ Lower pair

- No. of D.O.F. before pairing

$$2 \times 3 = 6$$

- Condition imposed by pairing

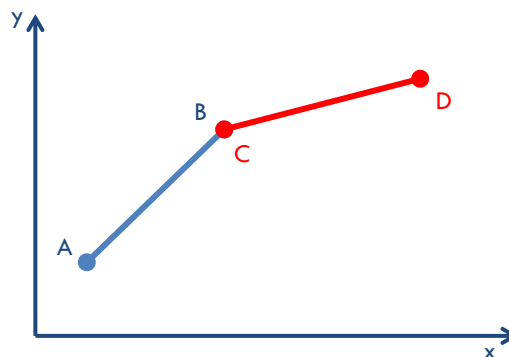
$$x_B = x_C, y_B = y_C$$

- No. of D.O.F. lost by pairing

$$2$$

- No. of D.O.F. after pairing

$$4$$



## 1.2. Kinematic pairs (cont.)



### □ Degrees of freedom lost by pairing

#### ➤ Lower pair

- No. of D.O.F. before pairing

$$2 \times 3 = 6$$

- Condition imposed by pairing

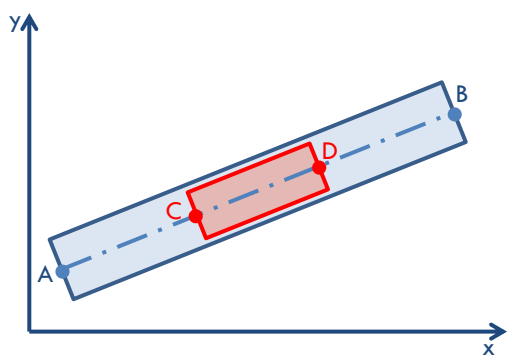
$$C \text{ on } AB, D \text{ on } AB$$

- No. of D.O.F. lost by pairing

$$2$$

- No. of D.O.F. after pairing

$$4$$



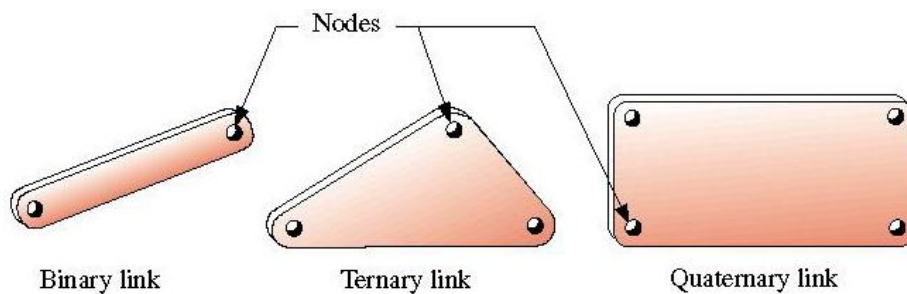
## 1.2. Kinematic pairs (cont.)



### □ Degrees of freedom lost by pairing

- Lower pair = 2
- Higher pair = 1

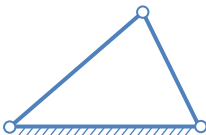
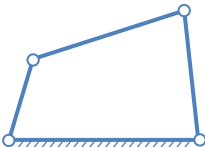
## 1.3. Types of links



## 1.4. Degrees of freedom of a mechanism



## □ Examples

		
■ D.O.F. before pairing	$3 \times 3 = 9$	$4 \times 3 = 12$
■ D.O.F. after grounding	$9 - 3 = 6$	$12 - 3 = 9$
■ D.O.F. lost by pairing	$3 \times 2 = 6$	$4 \times 2 = 8$
■ D.O.F. after pairing	$6 - 6 = 0$	$9 - 8 = 1$
	<b>Locked mechanism (Structure)</b>	<b>Mechanism with single input</b>

## 1.4. Degrees of freedom of a mechanism (cont.)



## □ Grübler Equation

$$N = 3(L-1) - 2P_l - P_h$$

L: No. of links

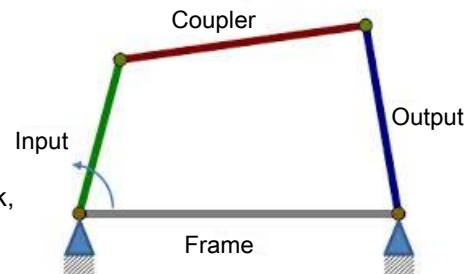
 $P_l$ : No. of lower pairs $P_h$ : No. of higher pair

## 1.5. Four-bar mechanism



### □ Types of four-bar mechanism

- Double-crank
  - Both input and output links are cranks
- Crank-lever (crank-rocker)
  - One of the input or output links is crank, whereas the other is lever
- Double-lever
  - Both input and output links are levers



## 1.5. Four-bar mechanism (cont.)



### □ Grashof's condition

- If  $S+L > P+Q$ , the mechanism is **double-rocker**
- If  $S+L \leq P+Q$ , it depends on which link is grounded

Fixed link	Mechanism Type
Shortest link	Double-crank
Adjacent to shortest	Crank-lever
Opposite to shortest	Double-lever