



Faculty of Engineering

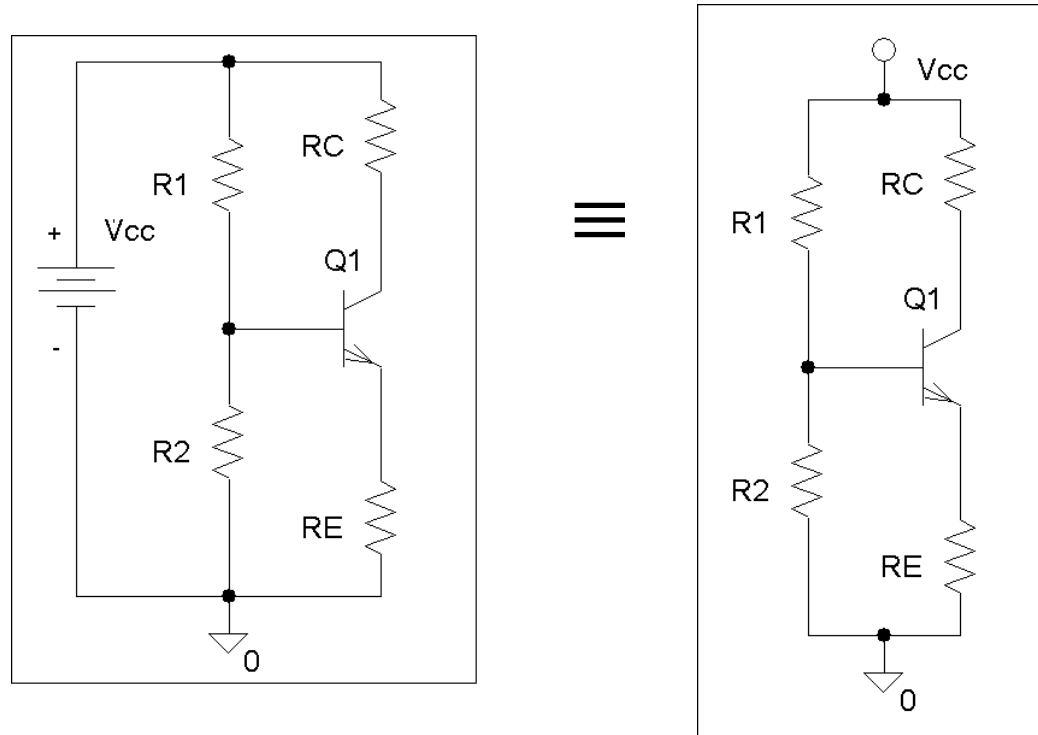
ECE 334: Electronic Circuits

Lecture 3:
BJT DC Circuit Analysis

BJT 'Q' Point (Bias Point)

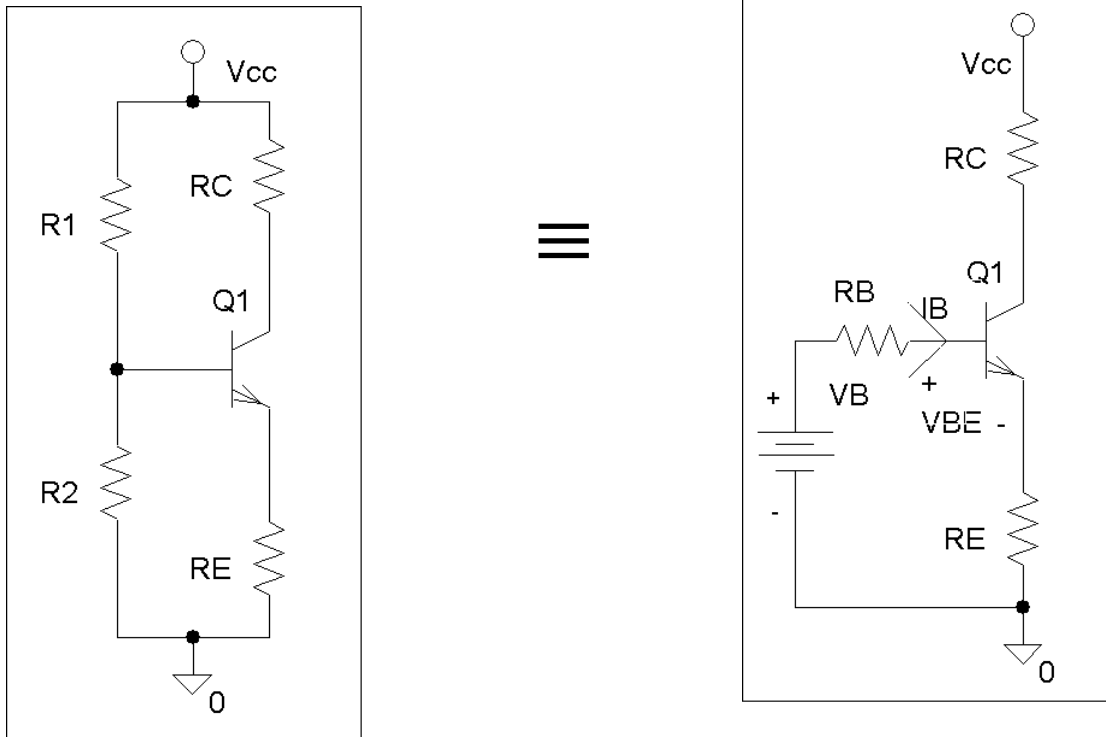
- Q point means Quiescent or Operating point
- Very important for amplifiers because wrong 'Q' point selection increases amplifier distortion
- Need to have a stable 'Q' point, meaning the the operating point should not be sensitive to variation to temperature or BJT β , which can vary widely

Example 1: Four Resistor bias Circuit for Stable 'Q' Point



By far best circuit for providing stable bias point

Example 1



$$V_B = V_{TH} = \frac{V_{CC} R_2}{R_1 + R_2}$$

$$R_B = R_{TH} = \frac{R_1 R_2}{R_1 + R_2}$$

Example 1 (2)

Applying KVL to the base-emitter circuit of the Thevenized Equivalent form

$$V_B - I_B R_B - V_{BE} - I_E R_E = 0 \quad (1)$$

$$\text{Since } I_E = I_B + I_C = I_B + \beta I_B = (1 + \beta)I_B \quad (2)$$

Replacing I_E by $(1 + \beta)I_B$ in (1), we get

$$I_B = \frac{V_B - V_{BE}}{R_B + (1 + \beta)R_E} \quad (3)$$

If we design $(1 + \beta)R_E \gg R_B$ (say $(1 + \beta)R_E \gg 100R_B$)

$$\text{Then } I_B \approx \frac{V_B - V_{BE}}{(1 + \beta)R_E} \quad (4)$$

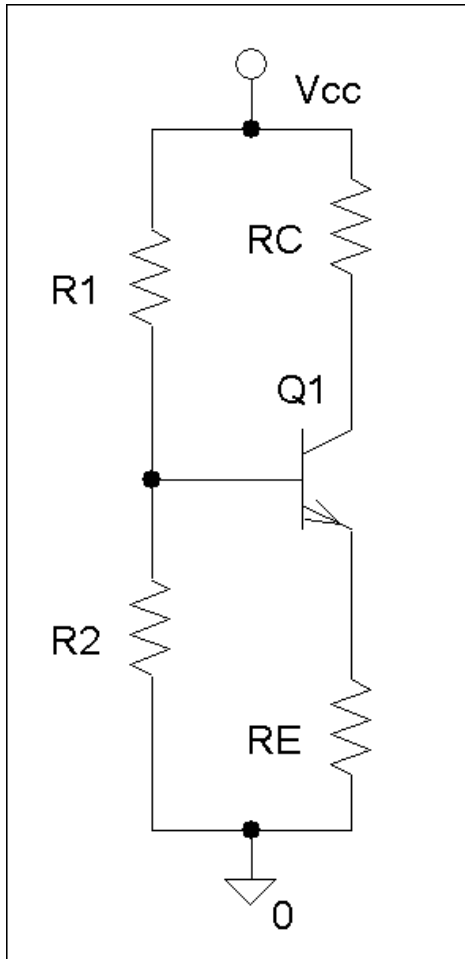
Example 1 (3)

$$\text{And } I_C = I_E \approx \frac{V_B - V_{BE}}{R_E} \quad (\text{for large } \beta) \quad (5)$$

Hence I_C and I_E become independent of β !

Thus we can setup a Q-point independent of β which tends to vary widely even within transistors of identical part number
(For example, β of 2N2222A, a NPN BJT can vary between 75 and 325 for $I_C = 1 \text{ mA}$ and $V_{CE} = 10\text{V}$)

Example 2



A 2N2222A is connected as shown with $R_1 = 6.8 \text{ k}\Omega$, $R_2 = 1 \text{ k}\Omega$, $R_C = 3.3 \text{ k}\Omega$, $R_E = 1 \text{ k}\Omega$ and $V_{CC} = 30\text{V}$. Assume $V_{BE} = 0.7\text{V}$. Compute V_{CC} and I_C for $\beta =$ i) 100 and ii) 300

Example 2 (2)

i) $\beta = 100$

$$V_B = V_{TH} = \frac{V_{CC} R_2}{R_1 + R_2} = \frac{30 * 1}{6.8 + 1} = 3.85V$$

$$R_B = R_{TH} = \frac{R_1 R_2}{R_1 + R_2} = \frac{6.8 * 1}{6.8 + 1} = 0.872k\Omega$$

$$I_B = \frac{V_B - V_{BE}}{R_B + (1 + \beta)R_E} = \frac{3.85 - 0.7}{0.872 + 101 * 1} = 30.92\mu A$$

$$I_{CQ} = \beta I_B = 3.09 \text{ mA}$$

$$I_{EQ} = (1 + \beta)I_B = 3.12 \text{ mA}$$

$$V_{CEQ} = V_{CC} - I_C R_C - I_E R_E = 30 - 3.09 * 3.3 - 3.12 * 1 = 16.68V$$

Example 2 (3)

i) $\beta = 300$

$$V_B = V_{TH} = \frac{V_{CC} R_2}{R_1 + R_2} = \frac{30 * 1}{6.8 + 1} = 3.85V$$

$$R_B = R_{TH} = \frac{R_1 R_2}{R_1 + R_2} = \frac{6.8 * 1}{6.8 + 1} = 0.872k\Omega$$

$$I_B = \frac{V_B - V_{BE}}{R_B + (1 + \beta)R_E} = \frac{3.85 - 0.7}{0.872 + 301 * 1} = 10.43\mu A$$

$$I_{CQ} = 300I_B = 3.13 \text{ mA}$$

$$I_{EQ} = (1 + \beta)I_B = 3.14 \text{ mA}$$

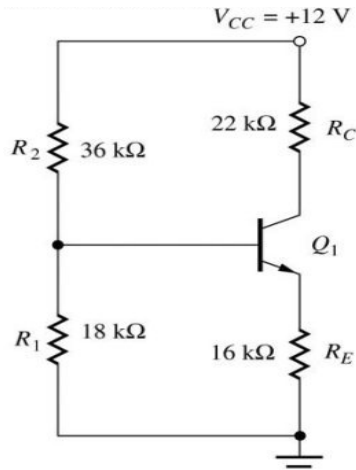
$$V_{CEQ} = V_{CC} - I_C R_C - I_E R_E = 30 - 3.13 * 3.3 - 3.14 * 1 = 16.53V$$

Example 2 (4)

	$\beta = 100$	$\beta = 300$	% Change
VCEQ	16.68 V	16.53 V	0.9 %
ICQ	3.09 mA	3.13 mA	1.29 %

The above table shows that even with wide variation of β the bias points are very stable.

Example 3



$$V_{EQ} = V_{CC} \frac{R_1}{R_1 + R_2} \quad R_{EQ} = R_1 \parallel R_2 = \frac{R_1 R_2}{R_1 + R_2}$$

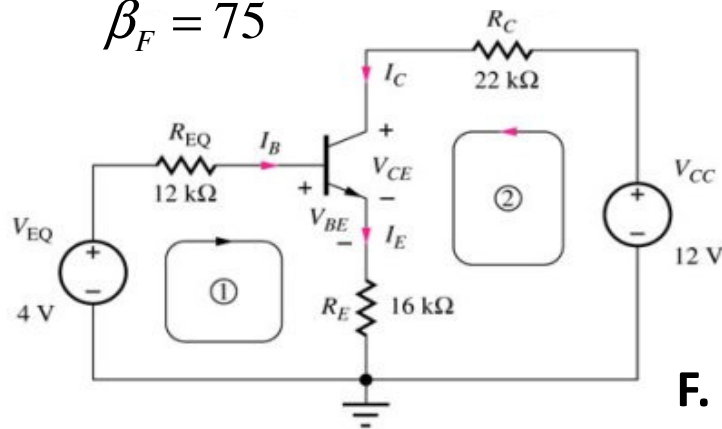
$$V_{EQ} = R_{EQ} I_B + V_{BE} + R_E I_E$$

$$4 = 12,000 I_B + 0.7 + 16,000 (\beta_F + 1) I_B$$

$$\therefore I_B = \frac{V_{EQ} - V_{BE}}{R_{EQ} + (\beta_F + 1) R_E} = \frac{4 \text{ V} - 0.7 \text{ V}}{1.23 \times 10^6 \Omega} = 2.68 \mu\text{A}$$

$$I_C = \beta_F I_B = 201 \mu\text{A}$$

$$\beta_F = 75$$



$$I_E = (\beta_F + 1) I_B = 204 \mu\text{A}$$

$$V_{CE} = V_{CC} - R_C I_C - R_E I_E$$

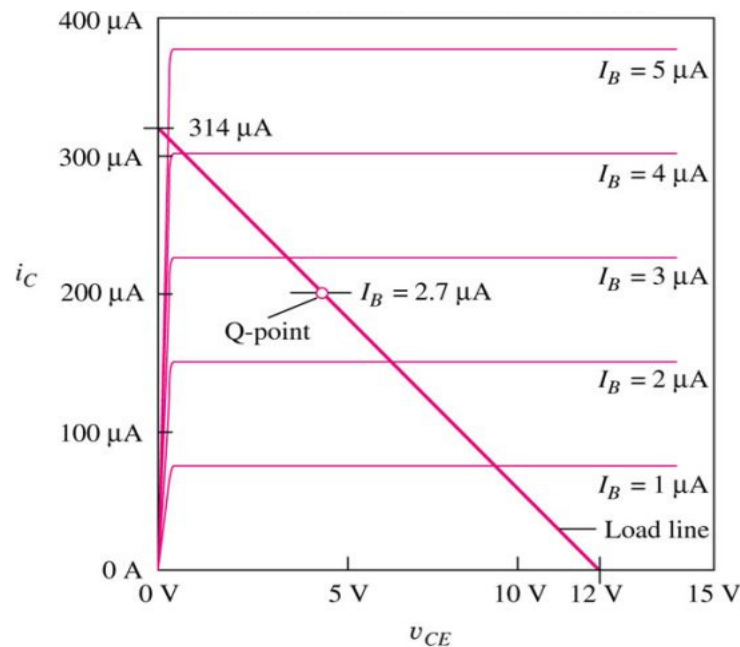
$$V_{CE} = V_{CC} - \left(R_C + \frac{R_E}{\alpha_F} \right) I_C = 4.32 \text{ V}$$

F. A. region correct - Q-point is (201 μA , 4.32 V)

Example 3 (2)

- All calculated currents > 0 , $V_{BC} = V_{BE} - V_{CE} = 0.7 - 4.32 = -3.62 \text{ V}$
- Hence, base-collector junction is reverse-biased,

$$V_{CE} = V_{CC} - \left(R_C + \frac{R_F}{\alpha_F} \right) I_C = 12 - 38,200 I_C$$



forward-active region operation

The two points needed to plot the load line are $(0, 12 \text{ V})$ and $(314 \mu\text{A}, 0)$.

The resulting load line is plotted on common-emitter output characteristics.

$I_B = 2.7 \mu\text{A}$, intersection of corresponding characteristic with load line gives Q-point.

Four-Resistor Bias Network for BJT: Design Objectives

- We know that

$$I_E = \frac{V_{EQ} - V_{BE} - R_{EQ} I_B}{R_E} \cong \frac{V_{EQ} - V_{BE}}{R_E} \quad \text{for} \quad R_{EQ} I_B \ll (V_{EQ} - V_{BE})$$

- This implies that $I_B \ll I_2$, so that $I_1 = I_2$. So base current doesn't disturb voltage divider action. Thus, Q-point is independent of base current as well as current gain.
- Also, V_{EQ} is designed to be large enough that small variations in the assumed value of V_{BE} won't affect I_E .
- Current in base voltage divider network is limited by choosing $I_2 \leq I_C/5$. This ensures that power dissipation in bias resistors is < 17 % of total quiescent power consumed by circuit and $I_2 \gg I_B$ for $\beta > 50$.

Four-Resistor Bias Network for BJT: Design Guidelines

- Choose Thévenin equivalent base voltage $\frac{V_{CC}}{4} \leq V_{EQ} \leq \frac{V_{CC}}{2}$
- Select R_1 to set $I_1 = 9I_B$. $R_1 = \frac{V_{EQ}}{9I_B}$
- Select R_2 to set $I_2 = 10I_B$. $R_2 = \frac{V_{CC} - V_{EQ}}{10I_B}$
- R_E is determined by V_{EQ} and desired I_C . $R_E \cong \frac{V_{EQ} - V_{BE}}{I_C}$
- R_C is determined by desired V_{CE} . $R_C \cong \frac{V_{CC} - V_{CE}}{I_C} - R_E$

Example 4

- **Problem:** Design 4-resistor bias circuit with given parameters.
- **Given data:** $I_C = 750 \mu\text{A}$, $\beta_F = 100$, $V_{CC} = 15 \text{ V}$, $V_{CE} = 5 \text{ V}$
- **Assumptions:** Forward-active operation region, $V_{BE} = 0.7 \text{ V}$
- **Analysis:** Divide $(V_{CC} - V_{CE})$ equally between R_E and R_C . Thus, $V_E = 5 \text{ V}$ and $V_C = 10 \text{ V}$

$$R_C = \frac{V_{CC} - V_C}{I_C} = 6.67 \text{ k}\Omega$$

$$R_E = \frac{V_E}{I_E} = 6.60 \text{ k}\Omega$$

$$V_B = V_E + V_{BE} = 5.7 \text{ V}$$

$$I_B = \frac{I_C}{\beta_F} = 7.5 \mu\text{A}$$

$$I_2 = 10I_B = 75.0 \mu\text{A}$$

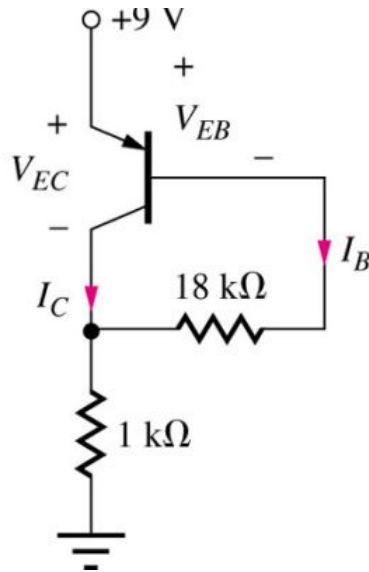
$$I_1 = 9I_B = 67.5 \mu\text{A}$$

$$R_1 = \frac{V_B}{9I_B} = 84.4 \text{ k}\Omega$$

$$R_2 = \frac{V_{CC} - V_B}{10I_B} = 124 \text{ k}\Omega$$

Example 5

- **Problem:** Find Q-point for *pn*p transistor in 2-resistor bias circuit with given parameters.
- **Given data:** $\beta_F = 50$, $V_{CC} = 9\text{ V}$
- **Assumptions:** Forward-active operation region, $V_{EB} = 0.7\text{ V}$
- **Analysis:**



$$9 = V_{EB} + 18,000 I_B + 1000 (I_C + I_B)$$

$$\therefore 9 = V_{EB} + 18,000 I_B + 1000 (51) I_B$$

$$\therefore I_B = \frac{9\text{ V} - 0.7\text{ V}}{69,000\ \Omega} = 120\ \mu\text{A}$$

$$I_C = 50 I_B = 6.01\ \text{mA}$$

$$V_{EC} = 9 - 1000 (I_C + I_B) = 2.88\ \text{V}$$

$$V_{BC} = 2.18\ \text{V}$$

Forward-active region operation is correct Q-point is : (6.01 mA, 2.88 V)